JEE MAIN 2024

Sample Paper - 2

Time Allowed: 3 hours General Instructions:

- All questions are compulsory.
- There are three parts and each part carries 30 questions where the first 20 questions are MCQs and the next 10 questions are numerical.
- Section-A within each part is compulsory. Attempt any 5 questions from section-B within each part.
- You will get 4 marks for each correct response and 1 mark will be deducted for an incorrect answer. However, there is no negative marking for Section-B (Numerical Questions)

PHYSICS (Section-A)

1. If force [F], acceleration [A] and time [T] are chosen as the fundamental physical quantities. **[4]** Find the dimensions of energy.

a) [F][A][T ⁻¹]	^{b)} [F][A ⁻¹][T]
c) [F][A][T]	d) [F][A][T ²]

2. A body travelling along a straight line traversed one-third of the total distance with a velocity v_1 . The remaining part of the distance was covered with a velocity v_2 for half the time and with velocity v_3 for the other half of time. The mean velocity averaged over the whole time of motion is:

a)	$\frac{3v_1(v_2\!+\!v_3)}{2v_1\!+\!v_2\!+\!v_3}$	b)	$rac{v_1(v_2\!+\!v_3)}{v_1\!+\!v_2\!+\!v_3}$
c)	$\frac{3v_1(v_2\!+\!v_3)}{4v_1\!+\!v_2\!+\!v_3}$	d)	$rac{v_1(v_2\!+\!v_3)}{4v_1\!+\!v_2\!+\!v_3}$

Four bodies A, B, C, and D are projected with equal speeds having angles of projection [4] 15°, 30°, 45°, and 60° with the horizontal respectively. The body having the shortest range is:

a) C	b) D
c) B	d) A

4. A body is projected upwards with a kinetic energy of 100 J. Taking the friction of air into [4] account, when it returns to the earth, its kinetic energy will be:

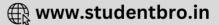
a) >1000 J	b) 100 J
c) < 100 J	d) > 100 J

5. A spring gun of spring constant 90 N/cm is compressed 12 cm by a ball of mass 16 g. If [4] the trigger is pulled, the velocity of the ball is:

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Maximum Marks: 300



^{a)} 40 ms ⁻¹	b) _{90 ms} -1
^{c)} 50 ms ⁻¹	d) _{9 ms} -1

6. A disc is rotating with an angular velocity ω_0 . A constant retarding torque is applied on it **[4]** to stop the disc. The angular velocity becomes $\left(\frac{\omega_0}{2}\right)$ after n rotations. How many more rotations will it make before coming to rest?

a) 2n	b) n

- c) $\frac{n}{3}$ d) $\frac{n}{2}$
- A small cylinder of 2 cm diameter is connected to a large cylinder of 20 cm diameter and [4] incompressible fluid is filled in the cylinders. If a force of 40 N is applied to the piston of the small cylinder, then the force exerted on the piston of the large cylinder will be:

a) 400 N	b) 8,000 N
c) 4,000 N	d) 800 N

8. An aluminum sphere is dipped into the water. Which of the following is true? [4]

^{a)} Buoyancy in water at 0 ^O C will be same as that in water at 4 ^O C.	 b) Buoyancy may be more or less in water at 4^OC depending on the radius of the sphere.
c) Buoyancy will be less in water at	d) Buoyancy will be more in water at
0 ⁰ C than that in water at 4 ⁰ C.	0 ⁰ C than that in water at 4 ⁰ C.

9. 540 calories of heat convert 1 cubic centimetre of water at 100°C into 1671 cm³ of steam ^[4] at 100°C. Then, the work done against atmospheric pressure is near:

a) 540 cal	b) Zero cal
c) 500 cal	d) 40 cal

10. A simple pendulum of length 1 m at sea level oscillates with time period T₁ s. If pendulum **[4]** is displaced upwards by $y = 3kt^2 + 5t + 1$, time period changes to T₂ s. If k is a constant equal to 2 m/s², then difference in time period will be, (g = 10 m/s²)

a) 0.82	b) 0.78
c) 0.29	d) 0.16

11. A charge Q is placed at the corner of a cube. The electric flux through all the six faces of [4] the cube is:

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a)
$$\frac{Q}{\varepsilon_0}$$
 b) $\frac{Q}{3\varepsilon_0}$



c)
$$\frac{Q}{8\varepsilon_0}$$

12. A current loop consists of two identical semicircular parts each of radius R, one lying in the [4] x, y-plane and the other in x, z-plane. If the current in the loop is i. The resultant magnetic field due to the two semicircular parts at their common centre is:

a)
$$\frac{\mu_0 i}{2\sqrt{2R}}$$
 b) $\frac{\mu_0 i}{4R}$
c) $\frac{\mu_0 i}{\sqrt{2R}}$ d) $\frac{\mu_0 i}{2R}$

13. The susceptibility of a paramagnetic material at 300 K is 1.4×10^{-5} . The material is cooled ^[4] and at a particular temperature, its susceptibility increased to 2.1×10^{-5} . What is the change in temperature of the material?

a) 200 K	b) 100 K
c) 300 K	d) 400 K

14. A metallic ring is attached to the wall room. When the north pole of a magnet is brought [4] near the ring, the induced current in the ring is:

a) in anticlockwise direction	b) zero
c) in clockwise direction	d) infinite

15. A series LCR circuit driven by 300 V at a frequency of 50 Hz contains a resistance R = 3 k Ω , [4] an inductor of inductive reactance X_L = 250 $\pi\Omega$ and an unknown capacitor. The value of

capacitance to maximize the average power should be: (Take $\pi^2 = 10$)

a) 25 $\mu { m F}$	b) 4 $\mu { m F}$
c) 40 <i>µ</i> F	d) 400 $\mu { m F}$

16. In an electromagnetic wave, the electric and magnetising fields are 100 V/m and 0.265 [4]A/m. The maximum energy flow is:

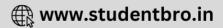
^{a)} 46.7 W/m ²	^{b)} 765 W/m ²
^{c)} 36.5 W/m ²	d) _{26.5} W/m ²

17. An electron accelerated under a potential difference V volt has a certain wavelength λ . [4] Mass of proton is some 2000 times of the mass of the electron. If the proton has to have the same wavelength λ , then it will have to be accelerated under a potential difference of:

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a) $\frac{V}{2000}$ volt	b) V volt
c) $\sqrt{2000}$ V volt	d) 2000 V volt



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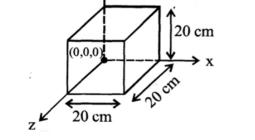
- 18. When an α -particle of mass m moving with velocity v bombards on heavy nucleus of charge Ze its distance of closest approach from the nucleus depends on m as:
 - a) $\frac{1}{\sqrt{m}}$ b) $\frac{1}{m^2}$ c) m d) $\frac{1}{m}$
- 20. When a diode is forward biased, it has a voltage drop of 0.5 V. The safe limit of current [4] through the diode is 10 mA. If a battery of emf 1.5 V is used in the circuit, the value of minimum resistance to be connected in series with the diode so that the current does not exceed the safe limit is:

a) 200Ω	b) 300Ω
c) 50Ω	d) 100Ω

PHYSICS (Section-B)

Attempt any 5 questions

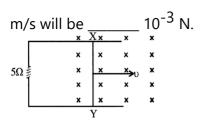
- 21. A cylindrical wire of radius 0.5 mm and conductivity 5×10^7 S/m is subjected to an electric [4] field of 10 mV/m. The expected value of current in the wire will be $x^3\pi$ mA. The value of x is _____
- 22. Expression for an electric field is given by $\vec{E} = 4000x^2 \hat{i} \frac{V}{m}$. The electric flux through the [4] cube of side 20 cm when placed in electric field (as shown in the figure) is _____ V cm.



23. A 1m long metal rod XY completes the circuit as shown in figure. The plane of the circuit is [4] perpendicular to the magnetic field of flux density 0.15 T. If the resistance of the circuit is 5 Ω , the force needed to move the rod in direction, as indicated, with a constant speed of 4

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[4]



- 24. Acceleration due to gravity on moon is $\frac{1}{6}$ th of the acceleration due to gravity on earth. If **[4]** the ratio of densities of earth (ρ_e) and moon (ρ_m) is $\left(\frac{\rho_e}{\rho_m}\right) = \frac{5}{3}$, then radius of moon R_m is kR_e . What will be the value of k?
- 25. At a given point of time the value of displacement of a simple harmonic oscillator is given [4] as $y = A \cos (30^{\circ})$. If amplitude is 40 cm and kinetic energy at that time is 200 J, the value of force constant is $1.0 \times 10^{X} \text{ Nm}^{-1}$. The value of x is _____.
- 26. If the ratio of magnifications produced by a simple microscope in near point adjustment [4] and far point adjustment is 6/5, then the focal length of the lens is _____ cm.
- 27. A current I = $3.36(1 + 2t) \times 10^{-2}$ A increases at a steady rate in a long straight wire. A [4] small circular loop of radius 10^{-3} m has its plane parallel to the wire and is placed at a distance of 1 m from the wire. The resistance of the loop is $8.4 \times 10^{-4} \Omega$. The magnitude of the induced current in the loop is (n $\times 10^{-11}$ A), then n is equal to?
- 28. A string fixed at both ends is vibrating in the lowest mode of vibration for which a point at **[4]** a quarter of its length from one end is a point of maximum displacement. The frequency of vibration in this mode is 100 Hz. What will be the frequency emitted when it vibrates in the next mode such that this point is again a point of maximum displacement.
- 29. The temperature of a thin uniform circular disc, of one metre diameter is increased by [4] 10° C. The percentage increase in moment of inertia of the disc about an axis passing through its centre and perpendicular to the circular face is _____. (linear coefficient of expansion = $11 \times 10^{-6}/^{\circ}$ C)
- 30. The breaking stress of a material is 10^6 N /m². If the density of the material is 3×10^3 [4] kg/m³, what should be the length of the material in metres so that it breaks by its own weight?

CHEMISTRY (Section-A)

- 31. Correct set of four quantum numbers for the valence (outermost) electron of rubidium (Z [4] = 37) is:
 - a) 5, 0, 0, $+\frac{1}{2}$ c) 5, 1, 1, $+\frac{1}{2}$ d) 5, 1, 0, $+\frac{1}{2}$
- 32. Two elements A and B have values of electronegativity respectively as 4 and 1.2, then the [4] compound A B will be:

a) both predominantely ionic and %

b) % covalent character less than 50%





	covalent character less than 50%		
	c) predominantely covalent	d) predominantely ionic	
33.	Which of the molecules listed have an sp ³ i. PCl ₃ ii. COCl ₂ iii. SF ₄	hybridized central atom?	[4]
	a) A only	b) A, B and C	
	c) A and C only	d) B and C only	
34.	C _p - C _v =		[4]
	^{a)} 8.314 J mol ⁻¹ deg ⁻¹	^{b)} 2 cal mol ⁻¹ deg ⁻¹	
	^{c)} both 2 cal mol ⁻¹ deg ⁻¹ and 8.314 J mol ⁻¹ deg ⁻¹	d) 8.314 cal mol ⁻¹ deg ⁻¹	
35.	What is the pH of the solution on mixing 10	00 mL of 0.1 M NH ₄ OH and 100 mL of 0.1 M	[4]
	$(NH_4)_3 PO_4? K_b \text{ for } NH_4OH = 1.8 \times 10^{-5}$		
	a) 9.5728	b) 9.2553	
	c) 9.2718	d) 8.7782	
36.	CrO ₅ reacts with H ₂ SO ₄ to give Cr ₂ (SO ₄) ₃ , of ClO ₅ in this reaction are:	H_2O and O_2 . Moles of O_2 liberated by 1 mole	[4]
	a) 1.75	b) 4.5	
	c) 1.25	d) 2.5	
37.	Moissan boron is form of boron.		[4]
	a) inert crystalline	b) inert amorphous	
	c) reactive amorphous	d) reactive crystalline	
38.	The most polar compound among the follo	owing is:	[4]
	a) F F F	b) F F F	







39. Which is the most suitable reagent among the following to distinguish compound (3) from **[4]** the rest of the compound?

i. $CH_3 - C = C - CH_3$ ii. $CH_3 - CH_2 - CH_2 - CH_3$ iii. $CH_3CH_2 - C = CH$ iv. $CH_3 - CH = CH_2$ a) Br_2 in CCl_4 b) $\frac{AgNO_3}{NH_4OH}$ c) Alk. KMnO₄ d) Br_2 in CH_3COOH

40. K_H value for Ar(g), CO₂(g), HCHO(g) and CH₄(g) are 40.39, 1.67, 1.83 \times 10⁻⁵ and 0.413 [4] respectively.

Arrange these gases in the order of their increasing solubility:

a) HCHO < CO ₂ < CH ₄ < Ar	b) Ar < CO ₂ < CH ₄ < HCHO
c) Ar < CH ₄ < CO ₂ < HCHO	d) HCHO < CH ₄ < CO ₂ < Ar

41. Boiling point of a 2% aqueous solution of a non-volatile solute A is equal to the boiling [4] point of 8% aqueous solution of a non-volatile solute B. The relation between molecular weights of A and B is

a) M _A = 4M _B	b) $M_B = 4M_A$
c) M _A = 8M _B	d) M _B = 8M _A

42. Using the data given below and find out which of the following is the strongest oxidising **[4]** agent.

$$\begin{split} E^{\ominus}_{\rm Cr_2O_7^{-}/Cr^{3+}} &= 1.33 \ V \ E^{\ominus}_{\rm Cl_2/Cl^{-}} &= 1.36 \ V \\ E^{\ominus}_{\rm MnO_4^{-}/Mn^{2+}} &= 1.51 \ V \ E^{\ominus}_{\rm Cr^{3+}/Cr} &= -0.74 \ V \\ a) \ Mn^2 + & b) \ Cl^- \\ c) \ MnO_4^{-} & d) \ Cr^{3+} \end{split}$$

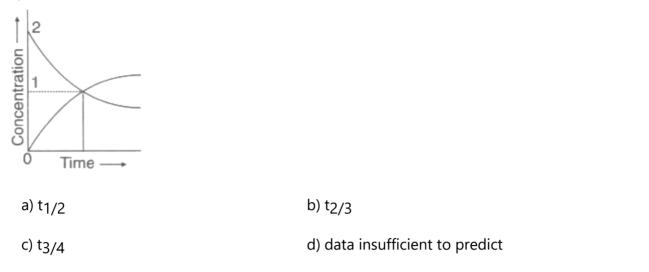
43. The accompanying figure depicts the change in concentration of species X and Y for the **[4]** reaction $X \rightarrow Y$, as a function of time. The point of intersection of the two curves

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represents:



- 44. Atomic number of Cr and Fe are Respectively 24 and 26, which of the following is **[4]** paramagnetic with the spin of an electron?
 - a) [Cr (NH₃)₆]³⁺ b) [Fe(CO)₅] c) [Cr(CO)₆] d) _{[Fe(CN)₆]⁴⁻}
- 45. Which of the following represents calcium chlorite?

a) Ca(ClO ₄) ₂	b) Ca(ClO ₃) ₂
c) Ca(ClO ₂) ₂	d) CaClO ₂

- 46. Among $[Ni(CN)_4]^{4-}$, $[Ni(PPh_3)_3Br]$ and $[Ni(dmg)_2]$ species, the hybridisation states of the **[4]** Ni-atoms are respectively:
 - a) sp³, sp³, dsp² c) sp³, dsp², dsp² d) dsp², dsp², dsp² d) dsp², sp³, dsp²

The correct order of $S_N 1$ reactivity is:

a) B > C > A b) B > A > C

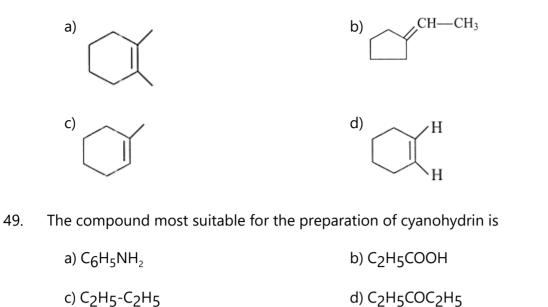
c) A > B > C d) C > B > A

48. OH on dehydration gives:



[4]

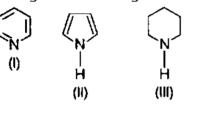
[4]



50. Arrange the following amines in the decreasing order of basicity:

[4]

[4]



a) > >	b) > >
c) > >	d) > >

CHEMISTRY (Section-B)

Attempt any 5 questions

51.	The number of spherical nodes in 4p orbital is/are	[4]
52.	In a chemical reaction, $A + 2B \stackrel{K}{\rightleftharpoons} 2C + D$, the initial concentration of B was 1.5 times of the concentration of A, but the equilibrium concentrations of A and B were found to be equal. The equilibrium constant (K) for the aforesaid chemical reaction is	[4]
53.	Ratio of σ -bonds and π -bonds in benzene molecule is:	[4]
54.	Total number of acidic oxides among N_2O_3 , NO_2 , N_2O_3 , NO_2 , N_2O_3 , C_2O_7 , SO_2 , CO , CaO , Na_2O and NO is	[4]
55.	Consider the following metal complexes: $[Co(NH_3)_6]^{3+}[CoCl(NH_3)_5]^{2+}$ $[Co(CN)_6]^{3-}[Co(NH_3)_5 (H_2O)]^{3+}$ The spin-only magnetic moment value of the complex that absorbs light with shortest wavelength is B.M. (Nearest integer)	[4]
56.	The number of statement(s) correct from the following for copper (at no. 29) is/are A. Cu (II) complexes are always paramagnetic B. Cu (I) complexes are generally colourless	[4]

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C. Cu (I) is easily oxidized

D. In Fehling solution, the active reagent has Cu (I)

- 57. A 100 mL solution was made by adding 1.43 g of Na₂CO₃·xH₂O. The normality of the [4] solution is 0.1 N. The value of x is _____. (The atomic mass of Na is 23 g/mol)
- 58. The abundances of isotopes ⁵⁴Fe, ⁵⁶Fe and ⁵⁷Fe are 5%, 90% and 5% respectively. The **[4]** atomic mass of Fe is _____.
- 59. Total number of planes in CH₄ which contain 3 atoms in a plane with carbon, is: [4]
- 60. 1 mole of ideal gas is allowed to expand reversibly and adiabatically from a temperature of [4] 27° C. The work done is 3 kJ mol⁻¹. The final temperature of the gas is K (Nearest integer). Given C_v= 20 J mol⁻¹K⁻¹.

MATHEMATICS (Section-A)

- - a) 50_{P17} b) 33! × 17!

c)
$$\frac{50!}{2}$$
 d) $50_{P_{33}}$

62. The sum of the solutions of the equation $|\sqrt{x} - 2| + \sqrt{x}(\sqrt{x} - 4) + 2 = 0(x > 0)$ is equal [4] to

a) 12	b) 9
c) 4	d) 10

63. The total number of functions, f:{1, 2, 3, 4} \rightarrow {1, 2, 3, 4, 5, 6} such that f(1) + f(2) = f(3), is equal to:

a) 108	b) 90
c) 60	d) 126

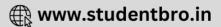
64. The sum of the last 30 coefficients in the expansion of $(1 + x)^{59}$ is

- a) ₂59 b) ₂56
- c) ₂57 d) ₂58
- 65. Let a, b, c, d and p be any non zero distinct real numbers such that $(a^2 + b^2 + c^2)p^2 2(ab$ ^[4] + bc + cd)p + $(b^2 + c^2 + d^2) = 0$. Then:

a) a, b, c, d are in A.P.	b) a, b, c, d are in G.P.
c) a, c, p are in A.P.	d) a, c, p are in G.P.

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66. If $f(x) = (\sqrt{4-x^2}-3)^2 + (\sqrt{4-x^2}+1)^3$, then the maximum value of f(x), is :

- a) 40 b) 25 c) 36 d) 28
- 67. A wire of length 20 m is to be cut into two pieces. A piece of length l_1 is bent to make a [4] square of area A_1 and the other piece of length l_2 is made into a circle of area A_2 . If $2A_1 + 3A_2$ is minimum then (πl_1) : l_2 is equal to:

68. $\int \frac{x^4}{(x-1)(x^2+1)} dx =$

- a) $\frac{x(x+2)}{2} + \frac{\log|x-1|}{2}$ $-\frac{\log|x^{2}+1|}{4} - \frac{\tan^{-1}x}{2} + c$ b) $\frac{x(x-2)}{2} - \frac{\log|x+1|}{2}$ $-\frac{\log|x^{2}-1|}{4} + \frac{\tan^{-1}x}{2} + c$ c) $\frac{x(x+2)}{2} + \frac{\log|x-1|}{2}$ $+\frac{\log|x^{2}+1|}{4} + \frac{\tan^{-1}x}{2} + c$ d) $\frac{x(x+2)}{2} + \frac{\log|x-1|}{2}$ $+\frac{\log|x^{2}+1|}{4} - \frac{\tan^{-1}x}{2} + c$
- 69. If length of the tangent drawn from each and every point on the curve $y = \sqrt{\lambda x^2}$ to the **[4]** circle $x^2 + y^2 = 36$ is 8 units, then λ is :
 - a) 30 b) 50 c) 100 d) 90
- 70. A stick of length I rests against the floor and a wall of a room. If the stick begins to slide [4] on the floor, then the locus of its middle point is
 - a) a straight lineb) an ellipsec) a parabolad) a circle
- 71. If one end of a focal chord AB of the parabola $y^2 = 8x$ is at $A\left(\frac{1}{\sqrt{2}}, -2\right)$, then the equation [4] of the tangent to it at B is:
 - a) 2x y 24 = 0c) 2x + y - 24 = 0b) x - 2y + 8 = 0c) 2x + y - 24 = 0c) x + 2y + 8 = 0
- 72. Solution of the differential equation $\left(e^{x^2} + e^{v^2}\right)y\frac{dy}{dx} + e^{x^2}(xy^2 x) = 0$, is : [4]

a)
$$e^{y^2}\left(y^2-1
ight)+e^{x^2}=C$$
 b) $e^{y^2}\left(x^2-1
ight)+e^{x^2}=C$

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[4]

c)
$$e^{x^2}(y-1) + e^{y^2} = C$$
 d) $e^{x^2}(y^2-1) + e^{y^2} = C$

- 73. The angle between a line with direction ratios proportional to (2, 3, 6) and a line joining (1, **[4]** -2, 4) to (-1, 1, -2) is:
 - a) $\cos^{-1}\left(\frac{31}{49}\right)$ b) $\cos^{-1}\left(\frac{21}{49}\right)$ c) $\cos^{-1}\left(\frac{3}{7}\right)$ d) $\cos^{-1}\left(\frac{6}{7}\right)$
- 74. Let PQR be a triangle. The points A, B and C are on the sides QR, RP and PQ respectively [4] such that $\frac{QA}{AR} = \frac{RB}{BP} = \frac{PC}{CQ} = \frac{1}{2}$. Then $\frac{\text{Area}(\triangle PQR)}{\text{Area}(\triangle ABC)}$ is equal to

a) $\frac{5}{2}$	b) 3
c) 2	d) 4

75. If the arithmetic mean of the numbers $x_1, x_2, x_3, ..., x_n$ is \bar{x} . Then the arithmetic mean of [4] numbers $ax_1 + b$, $ax_2 + b$, $ax_3 + b$, ... $ax_n + b$, Where a, b are two constants would be

a) na \bar{x} + nb	b) $ar{x}$
c) a \bar{x} + b	d) a $ar{x}$

76. Numbers 1 to 100 are written on slips of papers and are kept in a box. A draws one slip [4] randomly and replaces it. B then draws a slip randomly. What is the probability that B draws a bigger number?

a)
$$\frac{99}{20000}$$
 b) $\frac{99}{500}$
c) $\frac{49}{500}$ d) $\frac{99}{200}$

77. The maximum value of $(\cos \alpha_1) \cdot (\cos \alpha_2) \dots (\cos \alpha_n)$, under the restrictions [4] $0 \le \alpha_1, \alpha_2, \dots, \alpha_n \le \frac{\pi}{2}$ and $\cot \alpha_1 \cdot \cot \alpha_2 \dots \cot \alpha_n = 1$ is :

a) $\frac{1}{2^n}$	b) 1
C) $\frac{1}{2n}$	d) $\frac{1}{2^{n/2}}$

78. Find the equation of axis of the given hyperbola $\frac{x^2}{3} - \frac{y^2}{2} = 1$ which is equally inclined to [4] the axes?

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- a) y = x + 2c) y = x - 2b) y = x + 1d) y = x - 1
- 79. The set $(A \cup B \cup C) \cap (A \cap B' \cap C')' \cap C'$ is equal to

a) $B' \cap C'$ b) $A \cap C$

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d) B ∩ C'

80. If
$$S = \begin{cases} x \in [0, 2\pi] : \begin{vmatrix} 0 & \cos x & -\sin x \\ \sin x & 0 & \cos x \\ \cos x & \sin x & 0 \end{vmatrix} = 0 \end{cases}$$
 then $\sum_{x \in S} \tan \left(\frac{\pi}{3} + x\right)$ is equal to
a) $-2 - \sqrt{3}$
b) $-2 + \sqrt{3}$
c) $-4 - 2\sqrt{3}$
d) $4 + 2\sqrt{3}$

MATHEMATICS (Section-B) Attempt any 5 questions

81. Let $f : [0, \infty) \to R$ be a continuous, strictly increasing function such that $f^3(x) = \int_0^x t f^2(t) dt$. [4] If a normal is drawn to the curve y = f(x) with gradient $\frac{-1}{2}$, then find the intercept made by it on the y-axis.

- 82. Let g(x) is the only invertible function from R \longrightarrow R which satisfy the equation g³(x) (x³ + [4] 2) g²(x) + (2x³ + 1) g(x) - x³ = 0. Find the value of g'(8) · (g⁻¹)'(8).
- 83. Let $\vec{\mathbf{a}} = \hat{i} + 2\hat{j} + 3\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} \hat{k}$. If $\overrightarrow{\mathbf{c}}$ is a vector such that $\vec{a} \cdot \vec{c} = 11, \vec{b} \cdot (\vec{a} \times \vec{c}) = 27$ [4] and $\vec{b} \cdot \vec{c} = -\sqrt{3}|\vec{b}|$, then $|\vec{a} \times \vec{c}|^2$ is equal to
- 84. If the area of the region {(x, y): $|x^2 2| \le y \le x$ } is A, then 6A + $16\sqrt{2}$ is equal to _____. [4]
- 85. The shortest distance between the lines $\frac{x-2}{3} = \frac{y+1}{2} = \frac{z-6}{2}$ and $\frac{x-6}{3} = \frac{1-y}{2} = \frac{z+8}{0}$ is equal to [4]
- 86. Find the minimum number of tosses of a pair of dice so that the probability of getting the **[4]** sum of the digits on the dice equal to 7 on at least one toss is greater than 0.95. ($\log_{10}2 = 0.3010$; $\log_{10}3 = 0.4771$)
- 87. If $x = \cos 2\theta 2\cos^2 2\theta + 3\cos^3 2\theta 4\cos^2 \theta + \dots \infty$ [4] and $y - \cos 2\theta + 2\cos^2 2\theta + 3\cos^3 2\theta + 4\cos^4 2\theta + \dots \infty$ where $\theta \in (0, \frac{\pi}{4})$, then find least integral value of $(\frac{1}{x} + \frac{1}{y})$.
- 88. If tan A \cdot tan B = $\frac{1}{2}$. Then (5 3 cos 2A) (5 3 cos 2B) is equal to:
- 89. The number of elements in the set {A = $\begin{pmatrix} a & b \\ 0 & d \end{pmatrix}$: a, b, d \in {-1, 0, 1} and {I A}³ = I A³}, where I is 2 × 2 identity matrix, is:
- 90. Find the sum of all integral values of a where $a \in [-10, 10]$ such that the graph of the [4] function f(x) = ||x 2| a| 3 has exactly three x-intercepts.

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Sample Paper - 2

Solution

PHYSICS (Section-A)

1.

(d) [F][A][T²] Explanation: Given, Choosen fundamental quantities are, Force = F Acceleration = A Time = TDimensions of energy = ? $\mathbf{E} \propto \mathbf{F}^a \; \mathbf{A}^b \; \mathbf{T}^c$ $\Rightarrow [E] = [F^a] [A^b] [T^c]$ Now, $\Rightarrow [\mathrm{E}] = [\mathrm{ML}^2 \ \mathrm{T}^{-2}]$ $\left[\mathrm{A}
ight] = \left[\mathrm{M}^{\circ}\mathrm{L}\mathrm{T}^{-2}
ight]$ $[\mathrm{T}] = \left[\mathrm{M}^{\circ}\mathrm{L}^{\circ}T^{1}
ight]$ Substituting the values, $\left[\mathrm{ML}^2 \mathrm{~T}^{-2}
ight]^{-} = \left[\mathrm{MLT}^{-2}
ight]^a [T]^b [T]^c$ $\left[\mathrm{ML}^2 \ \mathrm{T}^{-2}
ight] = \left[\mathrm{M}^a \ \mathrm{L}^{a+b} \ \mathrm{T}^{-2a-2b+c}
ight]$ Now, comparing the exponents, a = 1 ...(i)a + b = 2 ...(ii)-2a - 2b + c = -2 ...(iii) From equation (i), (ii) and (iii) b = 2 - 1b = 1 And C = -2 + 2a + 2b= -2 + 2 + 2C = +2 Hence, $[E] = [FAT^2]$ 2.

-•

(c) $\frac{3v_1(v_2+v_3)}{4v_1+v_2+v_3}$

Explanation: Let S be the total distance travelled by the body. If t₁ is the time taken to cover first one-third distance, then

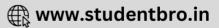
$$t_1=rac{S/3}{v_1}=rac{S}{3v_1}$$

Let t_2 be the time for each of the remaining two journeys. Then

$$\frac{2S}{3} = v_2 t_2 + v_3 t_2$$

or $t_2 = \frac{2S}{3(v_2 + v_3)}$
 \therefore Average velocity = $\frac{\text{total displacement}}{\text{total time}} = \frac{S}{t_1 + 2t_2}$
 $= \frac{S}{\frac{S}{3v_1} + \frac{4S}{3(v_2 + v_3)}} = \frac{3v_1(v_2 + v_3)}{v_2 + v_3 + 4v_1}$





(d) A

Explanation: From the formula of range for a given initial velocity,

Range, R = $\frac{u^2 \sin 2\theta}{\sigma}$

For a given initial velocity,

 $R \propto sin 2\theta$

4.

(c) < 100 J

Explanation: Kinetic energy = $\frac{1}{2}$ mv²

When the body returns to the earth its velocity will decrease due to friction of air i.e. some energy is lost in overcoming the friction. Thus, now its kinetic energy is less than 100J.

5.

(b) 90 ms⁻¹ Explanation: The kinetic energy of ball = potential energy of spring i.e. $\frac{1}{2}mv^2 = \frac{1}{2}kx^2$ $\therefore 16 \times 10^{-3} \times v^2 = \frac{90}{10^{-2}} \times (12 \times 10^{-2})^2$ or $v^2 = \frac{90 \times 144 \times 10^{-4}}{10^{-2} \times 16 \times 10^{-3}}$ or $v = 90 \text{ ms}^{-1}$ 6. (c) $\frac{n}{3}$

Explanation: Retarding torque is constant. Therefore, angular retardation say α will also be constant.

Applying, $\omega^2 = \omega_0^2 - 2\alpha\theta$ we get; $\left(\frac{\omega_0}{2}\right)^2 = \omega_0^2 - 2\alpha\theta_1$...(i) and $0 = \left(\frac{\omega_0}{2}\right)^2 - 2\alpha\theta_2$...(ii) Solving equations (i) and (ii), we get; $\theta_2 = \frac{\theta_1}{3}$

Therefore, the disc will make $\frac{n}{3}$ more rotations before coming to rest.

7.

(c) 4,000 N

Explanation: According to Pascal's law, the pressure of a fluid is transmitted in equal directions, i.e.,

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

$$\therefore F_2 = \left(\frac{F_1}{A_1}\right) \times A_2$$

$$= \frac{40}{\pi^{\frac{(2)^2}{4}}} \times \pi^{\frac{(20)^2}{4}} \dots (\because A = \pi^{\frac{d^2}{4}})$$

$$= 4000 \text{ N}$$

8.

(c) Buoyancy will be less in water at 0° C than that in water at 4° C.

)

Explanation: As buoyancy at 0^oC, $F_b = V \rho_0 g$ and buoyancy at 4^oC, $F'_b = V \rho_4 g$

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 $\frac{F_b}{E'} = \frac{\rho_0}{\rho_4} < 1$ (Density of water at 4^oC is maximum)

 $So, F_b < F'_b$

(d) 40 cal **Explanation:** Amount of heat given = 540 calories Change in volume $\Delta V = 1670$ c.c Atmospheric pressure P = 1.01×10^6 dyne/cm² Work done against atmospheric pressure W = $P\Delta V = \frac{1.01 \times 10^6 \times 1670}{4.2 \times 10^7} \approx 40$ cal

10.

(b) 0.78

Explanation: Vertical displacement

 $y = 3kt^2 + 5t + 1$

Differentiating above equation w.r.t. time,

$$\frac{dy}{dt} = 6$$
kt + 5

Differentiating again with respect to time,

$$\frac{d^2y}{dt^2} = 6k + 5$$

i.e., a = 6k + 5
a = 6 × 2 + 5 ...(: k = 2 m/s²)
= 17 m/s²

Total effective acceleration after displacement is given by,

g' = g + a = 10 + 17 = 27 m/s²
T₁ =
$$2\pi \sqrt{\frac{l}{g}}$$
; T₂ = $2\pi \sqrt{\frac{l}{g'}}$

... Difference in time period,

$$T_{1} - T_{2} = 2\pi\sqrt{l} \left(\frac{1}{\sqrt{g}} - \frac{1}{\sqrt{g'}}\right) = 2\pi \left(\frac{1}{\sqrt{10}} - \frac{1}{\sqrt{27}}\right)$$

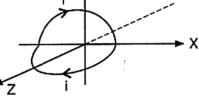
= 0.78

11. (a)
$$\frac{Q}{\varepsilon_0}$$

Explanation: According to the Gauss' theorem, the electric flux through a close surface in $\frac{Q}{\varepsilon_0}$.

12. (a)
$$\frac{\mu_0 i}{2\sqrt{2R}}$$

Explanation:



The loop mentioned in the question must look like one as shown in the figure.

The magnetic field at the centre due to semicircular loop lying in the X-Y plane, $B_{xy} = \frac{1}{2} \left(\frac{\mu_0 i}{2R} \right)$ negative Z-direction.

Similarly, field due to loop in X-Z plane $B_{xz} = \frac{1}{2} \left(\frac{\mu_0 i}{2R} \right)$ in negative Y-direction.

 \therefore The magnitude of the resultant magnetic field,

$$egin{aligned} B &= \sqrt{B_{xy}^2 + B_{xz}^2} = \sqrt{\left(rac{\mu_0 i}{4R}
ight)^2 + \left(rac{\mu_{(L} i}{4R}
ight)^2
ight)^2} \ &= rac{\mu_0 i}{4R} \sqrt{2} = rac{\mu_0 i}{2\sqrt{2R}} \end{aligned}$$

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(b) 100 K

Explanation: As per Curie law,

- $$\begin{split} \chi \propto \frac{1}{T} \\ \therefore \frac{\chi_2}{\chi_1} &= \frac{T_1}{T_2} \\ \therefore \frac{2.1 \times 10^{-5}}{1.4 \times 10^{-5}} &= \frac{300}{T_2} \\ \frac{3}{2} &= \frac{300}{T_2} \\ \therefore T_2 &= \frac{600}{3} \\ &= 200 \text{ K} \\ \therefore \text{ Change in temperature} \\ &= T_1 T_2 \\ &= 300 200 \\ &= 100 \text{ K} \end{split}$$
- 14. (a) in anticlockwise direction
 - **Explanation:** As it is seen from the magnet side induced current is will be anticlockwise.
- 15.

(b) 4 μF

Explanation: Power will be maximum at resonance

At resonance
$$X_L = X_C \Rightarrow L\omega = \frac{1}{C\omega}$$

 $\Rightarrow 250 \ \pi = \frac{1}{2\pi(50)C} \Rightarrow C = 4 \times 10^{-6}$

16.

(d) 26.5 W/m²

Explanation: Here, the amplitude of the electric field, $E_0 = 100$ V/m; the amplitude of the magnetic field, $H_0 = 0.265$ A/m. We know that the maximum rate of energy flow,

 $s = e_0 \times H_0 = 100 \times 0.265 = 26.5 \text{ W/m}^2$

17. (a) $\frac{V}{2000}$ volt

Explanation:
$$\lambda_e = \lambda_p$$

or $\frac{h}{\sqrt{2m_e Q_e V}} = \frac{h}{\sqrt{2m_p Q_p V_p}}$
 $\therefore m_e Q_e V = m_p Q_p V_p$
 $\therefore V_p = \left(\frac{m_e}{m_p}\right) \left(\frac{Q_e}{Q_p}\right) V = \left(\frac{1}{2000}\right) (1)V = \frac{V}{2000}$ volt

18.

(d) $\frac{1}{m}$

Explanation: As we know that,

(K.E.)_{initial} = (P.E)_{closest} approach

$$rac{1}{2}mv^2 = rac{2Ze^2}{4\piarepsilon_0 r_0} \ \Rightarrow r_0 \propto rac{1}{m}$$

19.

(b) 4.25 MeV

Explanation: For the given nuclear reaction, amount of energy released Q = $(m_A - m_B - m_D)$ × 931.5 MeV = (238.05079 - 234.04363 - 4.00260) × 931.5 or, Q = 4.25 MeV 20.

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(d) 100Ω

Explanation: According to the question, when the diode is forward biased, $V_{diode} = 0.5 V$

Safe limit of current, I = 10 mA = 10^{-2} A R_{min} = ? Voltage through resistance V_R = 1.5 - 0.5 = 1 volt iR = 1 (= V_R) \therefore R_{min} = $\frac{1}{i} = \frac{1}{10^{-2}} = 100\Omega$

21. 5.0

Explanation:

Given: Conductivity of wire, $\sigma = 5 \times 10^7$ S/m Radius of wire, r = 0.5 mm $= 5 \times 10^{-4}$ m Electric field, $E = 10 \times 10^{-3}$ V/m $J = \sigma E = 10 \times 10^{-3} \times 5 \times 10^7 \Rightarrow J = 5 \times 10^5$ Since, $J = \frac{i}{A} \Rightarrow \frac{i}{A} = 5 \times 10^5$ $\Rightarrow i = 5 \times 10^5 \times \pi r^2 = 5 \times 10^5 \times \pi \times (5 \times 10^{-4})^2$ $= 125\pi \times 10^{-3}$ A $\therefore i = 125\pi$ mA $\therefore i = 5^3\pi$ mA $\therefore x = 5$

22. 640.0

Explanation: Flux through surface x = 0, y = 0, y = 20 cm, z = 0 and z = 20 cm will be zero as for these surface $\vec{E} \perp \vec{A}$

Flux through surface (x = 0.2 m) = $4000 \times 0.2^2 \times 0.2^2 = 6.4$ Vm = 640 Vcm 23. 18.0

Explanation:

Magnetic field
$$\ell F = B$$
 ($\because \varepsilon = iR$)
= $\left(\frac{\varepsilon}{R}\right) \ell B = \left(\frac{vB\ell}{R}\right) \ell B = \frac{vB^2\ell^2}{R} = \frac{4}{5} \times \left(\frac{15}{100}\right)^2 \times 1^2$
= $\frac{4}{5} \times \frac{225}{10^4} = 18 \times 10^{-3}$ N ($\because \varepsilon = vB\ell$)

24. 0.28

Explanation: $g = \frac{4}{3}\pi G\rho R$ $g \propto \rho R$ $\therefore \frac{g_e}{g_m} = \frac{\rho_e}{\rho_m} \times \frac{R_e}{R_m}$ $\therefore \frac{6}{1} = \frac{5}{3} \times \frac{R_e}{R_m}$ $\therefore R_m = \frac{5}{18}R_e$ $\therefore k = \frac{5}{18} = 0.28$ 25. 4.0 Explanation: General equation for displacement is x = A sin ($\omega t + \phi$) Comparing with given equation, y = A cos (30^o) $\omega t + \phi = 30^o$ $\therefore x = 40 \times \frac{\sqrt{3}}{2} \Rightarrow 20\sqrt{3} \text{ cm and } A = 40 \text{ cm}$ Kinetic energy, K .E = $\frac{1}{2}k \left(A^2 - x^2\right) = 200$ $200 = \frac{1}{2}k \left(\frac{1600 - 1200}{100 \times 100}\right)$ $\Rightarrow 400 \times 100 \times 100 = k \times 400 \Rightarrow k = 10^4$ $\therefore x = 4$ 26. 5 Explanation: $\frac{\text{Given: } 6}{5} = \frac{\left(1 + \frac{D}{f}\right)}{\frac{D}{f}}$ or $\frac{6}{5} = \left(\frac{f}{D} + 1\right)$ or $\frac{f}{D} = \frac{6}{5} - 1 = \frac{1}{5}$ or $f = \frac{D}{5} = 5$ cm.

27.5

Explanation:

I = 3.36[1 + 2t] × 10⁻²A, R = 1m, radius of loop x = 10⁻³m The magnetic field at the location of loop at a distance r = 1m from wire $B = \frac{\mu_0 I}{2\pi r}$ perpendicular to the plane of loop The magnetic flux linked with the loop $\phi = BA \cos 0^\circ = BA = B\pi x^2 = \frac{\mu_0 I}{2\pi r} (\pi x^2)$ Induced emf, $e = -\frac{d\phi}{dt} = -\frac{d}{dt} \left(\frac{\mu_0 I}{2\pi r} \pi x^2\right)$ $= \frac{\mu_0}{2r} x^2 \cdot \frac{dI}{dt}$ Current induced, $I = \frac{e}{R} = \frac{\mu_0 x^2}{2rR} \frac{dI}{dt}$ $= \frac{\mu_0 x^2}{2rR} \frac{d}{dt} [3.36(1+2t) \times 10^{-2}]$ $= \frac{\mu_0 x^2}{2rR} [3.36 \times 2 \times 10^{-2}]$ Here r = 1m, x = 10⁻³ m, R = 8.4 × 10⁻⁴ Ω $I = \frac{4\pi \times 10^{-7} \times (10^{-3})^2 \times 2 \times 3.36 \times 10^{-2}}{2 \times 1 \times 8.4 \times 10^{-4}}$ $= 16\pi \times 10^{-12} A = 5.0 \times 10^{-11} A$ 28. 300

Explanation:

Point of maximum displacement mean antinode. The situation is shown in figure.

For initial situation,
$$\frac{2\lambda}{2} = 1$$

 $f = \frac{v}{\lambda} = \frac{v}{L} = 100 \text{ Hz}$
For final situation, $\frac{6\lambda}{2} = L$

$$f' = \frac{v}{\lambda} = \frac{3v}{L} = 300 \text{ Hz}$$

29. 0.022

Explanation:

$$egin{aligned} &I \propto r^2 \Rightarrow \Delta l = 2r(\Delta r) \ & ext{or} \ rac{\Delta I}{I} = rac{2r(\Delta r)}{r^2} = rac{2(\Delta r)}{r} \ & ext{but} \ rac{\Delta r}{r} = (lpha)(\Delta t) \ &\therefore rac{\Delta I}{I} imes 100 = 2(lpha)(\Delta t) 100 = 2\left(11 imes 10^{-6}
ight)(10)(100) = 0.022 \end{aligned}$$

30. 33.3

Explanation:

Stress = $\frac{\text{weight}}{\text{area}} = \frac{mg}{A} = \frac{Vdg}{A} = \frac{ALdg}{A} = Ldg$ $\therefore L = \frac{\text{breaking stress}}{dg} = \frac{10^6}{3 \times 10^3 \times 10} = 33.3 \text{ m.}$

CHEMISTRY (Section-A)

31. **(a)** 5, 0, 0, $+\frac{1}{2}$

Explanation: $_{37}$ Rb = 2, (2, 6)(2, 6, 10)(2, 6)(1) = $_{1s^2}$, $_{2s^22p^6}$, $_{3s^23p^63d^{10}}$, $_{4s^24p^6}$, $_{5s^1}$ Valence electron is $_{5s^1}$



: n = 5, I = 0, m = 0, $s = +\frac{1}{2}(or -\frac{1}{2})$

- 32. (a) both predominantely ionic and % covalent character less than 50% **Explanation:** both predominantely ionic and % covalent character less than 50%
- 33. (a) A only

Explanation: PCl₃ has sp³ hybridised.

34.

(c) both 2 cal mol⁻¹ deg⁻¹ and 8.314 J mol⁻¹ deg⁻¹ **Explanation:** $C_p - C_v = R = 2 \text{ cal mol}^{-1} \text{ deg}^{-1}$ $= 8.314 \text{ J mol}^{-1} \text{ deg}^{-1}$ 35. (d) 8.7782 Explanation: For basic buffer mixture $pOH = pK_a + log \frac{[Conjugate acid]}{[Base]}$ $[base] = [NH_4OH] = \frac{100 \times 0.1}{200} = 0.05$ [conjugate acid] = $[NH_4^+] = \frac{100 \times 0.1 \times 3}{200} = 0.15$

 $(NH_4)_3 PO_4$ gives three ions of NH_4^+ (conjugate acid)

∴ pOH =
$$-\log 1.8 \times 10^{-5} + \log \frac{0.15}{0.05}$$

= 4.7447 + 0.4771 = 5.2218
∴ pH = 14 - 5.2218 = 8.7782

Explanation: 1.75

37.

(c) reactive amorphous **Explanation:** reactive amorphous

38. **(a)**

Explanation: Among the substituents attached to the given compounds, fluorine has maximum electronegativity, so it will push the electron pair towards itself. In this option, the compound has the two F groups along the same direction, thus net dipole moment will increase in this direction, and therefore it will exhibit maximum polarity. Hence the compound in this option has maximum polarity.

39.

(b) $\frac{AgNO_3}{NH_4OH}$ Explanation: $\frac{AgNO_3}{NH_4OH}$

40.

(b) Ar < CO₂ < CH₄ < HCHO

Explanation: The unit of K_H should have been reported. However, HCHO being polar will be more soluble. CH_4 is more soluble than CO_2 .

41.

```
(b) M_B = 4M_A

Explanation: \Delta_A T_b = \frac{2}{M_A \times 100} \times 1000 \times K_b

\Delta_B T_b = \frac{8}{M_B \times 100} \times 1000 \times K_b

Given, \Delta_A T_b = \Delta_B T_b

\Rightarrow \frac{2}{M_A} = \frac{8}{M_B} \Rightarrow M_B = 4M_A
```

42.

(c) MnO_4^-

Explanation: MnO_4^-

43. (a) t_{1/2}

Explanation: The inter-section point indicate that half of the reactant X is converted into Y.

44. **(a)** [Cr (NH₃)₆]³⁺

Explanation: Odd electrons, ions, and molecules are paramagnetic.

In Cr(CO)₆ molecule 12 electrons are contributed by CO group and it contains no odd electron.

 $Cr \rightarrow 3d^{5}4s^{1}$

Fe(CO)₅ molecule also does not contain an odd electron.

 $Fe \to 3d^{6}4s^{2}$

In $[Fe(CN)_6]^{4-}$ ion $Fe(+II) \rightarrow 3d^64s^0$

∴ No odd electrons.

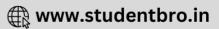
In $[Cr(NH_3)_6]^{3+}$ ion $Cr(+III) \rightarrow 3d^34s^0$

This ion contains an odd electron so it is paramagnetic.

45.

(c) Ca(ClO₂)₂





Explanation: Since the valency of calcium is 2 and a chlorite ion is ClO_2^- , therefore calcium chlorite is Ca(ClO₂)₂.

46. **(a)** sp³, sp³, dsp²

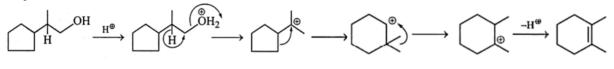
Explanation: sp³, sp³, dsp²

47. (a) B > C > A

Explanation: Substrate which form more stable cation they leads to major product. 48. (a)



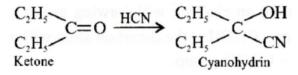
Explanation:



49.

(d) C₂H₅COC₂H₅

Explanation: Ketone reacts with HCN to form an addition product, known as cyanohydrin compound.

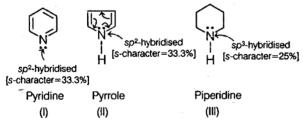


50.

(b) ||| > | > ||

Explanation:

The % of 5-character in the given amines are as follows:



Therefore, piperidine (III) having minimum % s-character is most basic. Among the rest, pyridine (I) and pyrrole (II) the lone pair of electrons of N in pyrrole (II) is involved in delocalisation and follows (4n + 2) n aromatic (n = 1) system. So, the N-atom of pyrrole (II) will show least basicity. Thus, the order of basicity is as follows: (III) > (I) > (I)

CHEMISTRY (Section-B)

51. 2

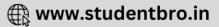
Explanation:

The number of spherical or radial nodes in an orbital = (n - l - 1)4p orbital (n = 4, l = 1) has 2 spherical nodes.

52.4

Explanation:





For the given chemical reaction, $A + 2B \implies 2C + D$ • • [x = degree of dissociation] $1.5a_{0}$ At. t = 0 a_0 $1.5a_0 - 2x$ 2x $t = t_{eq}$ $a_0 - x$ Given, at equilibrium. [A] = [B] $a_0 - x = 1.5a_0 - 2x$ $x = 0.5a_{0}$ \therefore [A] = a₀ - x = a₀ - 0.5a₀ = 0.5a₀ $[B] = 1.5a_0 - 2x = 1.5a_0 - 2 \times 0.5a_0 = 0.5a_0$ $[C] - 2x = 2 \times 0.5a_0 = a_0$ $[D] = x = 0.5a_0$ Now, $K = \frac{[C]^2[D]}{[A][B]^2}$ Now, substituting the values in above equation, we get $K = rac{(a_0)^2 imes (0.5a_0)}{(0.5a_0) imes (0.5a_0)} = 4$ 53.4 **Explanation:** 12σ bonds, 3π bonds 54.4

Explanation: Acidic oxides are N2O3, NO2, Cl2O7, SO2

Basic oxides are CaO, Na₂O

Neutral Oxides are CO, NO, N₂O

55. 2.0

Explanation:

The complex that absorbs the light with shortest wavelength is the most stable complex formed by Co^{3+} and strong field ligand CN^{-} .

 \therefore Octahedral low spin Co³⁺ complex, [Co (CN)₆]³⁻ has the electronic configuration = $t_{2q}^6 e_g^1$: $M_{S,O_1} = \sqrt{n(n+2)} = \sqrt{1(1+2)} = \sqrt{3} = 1.732 \approx 2$

56. 3.0

Explanation:

A, B, C are correct and D is incorrect because Fehling solution has Cu(II).

57.10

Explanation:

Normality =
$$\frac{\text{No. of equivalents of solute}}{\text{Volume of solution (in L)}}$$

 $0.1 = \frac{1.43}{\frac{(106+18x)}{2} \times 0.1} \Rightarrow \frac{106+18x}{2} = 143$
 $\Rightarrow 18x = 286 - 106 = 180 \Rightarrow x = 10$
58. 55.95
Explanation:
Atomic mass of Fe = $\frac{\sum A_1 \cdot X_1}{\sum X_T}$
 $= \frac{54 \times 5 + 56 \times 90 + 57 \times 5}{5 + 90 + 5} = 55.95$
59. 6

```
Explanation:
```

59

Total six planes contain HCH atoms in a plane.

60. 150

Explanation: q = 0, $\triangle U = w$ 1 × 20 × [T₂ - 300] = -3000 T₂ - 300 = -150 \Rightarrow T₂ = 150 K

MATHEMATICS (Section-A)

61.

(**d**) ⁵⁰P₃₃

Explanation: Given that f is bijective function and $f(3) \ge f(9) \ge f(15) \ge f(21) \ge ... \ge f(99)$ So, all elements 3, 9, 15... 99 i.e. 17 elements as 1 choice. Remaining 50 - 17 = 33 elements has taken from 50 elements.

 \therefore Number of ways = ${}^{50}P_{33}$

: Sum of roots = 9 + 1 = 10

62.

(d) 10 Explanation: Given equation is $|\sqrt{x} - 2| + \sqrt{x}(\sqrt{x} - 4) + 2 = 0$ $\Rightarrow |\sqrt{x} - 2| + x - 4\sqrt{x} + 4 = 2$ $\Rightarrow |\sqrt{x} - 2| + (|\sqrt{x} - 2|)^2 = 0$ $\Rightarrow (|\sqrt{x} - 2|)^2 + |\sqrt{x} - 2| - 2 = 0$ Let $|\sqrt{x} - 2| = y$, then above equation reduced to $y^2 + y - 2 = 0 \Rightarrow y^2 + 2y - y - 2 = 0$ $\Rightarrow y(y + 2) - 1(y + 2) = 0 \Rightarrow (y + 2) (y - 1) = 0$ $\Rightarrow y = 1, -2$ $\therefore y = 1 [\because y = |\sqrt{x} - 2| \ge 0]$ $\Rightarrow |\sqrt{x} - 2| = 1$ $\Rightarrow \sqrt{x} - 2 = \pm 1$ $\Rightarrow \sqrt{x} = 3 \text{ or } 1$ $\Rightarrow x = 9 \text{ or } 1$

63.

(b) 90

Explanation: Given A = {1, 2, 3, 4} B = {1, 2, 3, 4, 5, 6} Here f(3) can be 2, 3, 4, 5, 6 f(3) = 2, (f(1), f(2)) \rightarrow (1, 1) \rightarrow Total 6 cases f(3) = 3, (f(1), f(2)) \rightarrow (1, 2), (2, 1) \rightarrow 2 × 6 = Total 12 cases f(3) = 4,(f(1), f(2)) \rightarrow (1, 3), (3, 1), (2, 2) \rightarrow 3 × 6 = Total 18 cases f(3) = 5, (f(1), f(2)) \rightarrow (1, 4), (4, 1), (2, 3), (3, 2) \rightarrow 4 × 6 = Total 24 cases f(3) = 6,(f(1), f(2)) \rightarrow (1, 5), (5, 1), (2, 4), (4, 2), (3, 3) \rightarrow 5 × 6 = Total 30 cases Total number of cases = 6 + 12 + 18 + 24 + 30 = 90

(**d**) 2⁵⁸

Explanation: Required sum = ${}^{59}C_{30} + {}^{59}C_{31} + {}^{59}C_{32} + ... + {}^{59}C_{59}$ = $\frac{1}{2} [({}^{59}C_{29} + {}^{59}C_{30}) + ({}^{59}C_{28} + {}^{59}C_{31}) + ... + ({}^{59}C_0 + {}^{59}C_{59})] ... [: `^{n}C_{r} = {}^{n}C_{n-r}]$ = $\frac{1}{2} ({}^{59}C_0 + {}^{59}C_1 + {}^{59}C_2 + ... + {}^{59}C_{59})$ = $\frac{1}{2} (259) = 2{}^{58}$

65.

(**b**) a, b, c, d are in G.P.

Explanation: Rearrange given equation, we get

$$(a^{2}p^{2} - 2abp + b^{2}) + (b^{2}p^{2} - 2bcp + c^{2}) + (c^{2}p^{2} - 2cdp + d^{2}) = 0$$

$$\Rightarrow (ap - b)^{2} + (bp - c)^{2} + (cp - d)^{2} = 0$$

$$\therefore ap - b = bp - c = cp - d = 0$$

$$\Rightarrow \frac{b}{a} = \frac{c}{b} = \frac{d}{c} \therefore a, b, c, d \text{ are in GP.}$$

66.

(d) 28 Explanation: 28

67.

(b) 6 : 1 **Explanation:** Since, given $l_1 + l_2 = 20 \Rightarrow \frac{\mathrm{d}l_2}{\mathrm{d}l_1} = -1$ Now, $A_1 = \left(\frac{l_1}{4}\right)^2$ and $A_2 = \pi \left(\frac{l_2}{2\pi}\right)^2$ Let S = 2A₁ + 3A₂ = $\frac{l_1^2}{8} + \frac{3l_2^2}{4\pi}$ For max or min $rac{\mathrm{ds}}{\mathrm{d}l_1} = 0 \Rightarrow rac{2l_1}{8} + rac{6l_2}{4\pi} \cdot rac{\mathrm{d}l_2}{\mathrm{d}l_1} = 0$ $\Rightarrow \frac{l_1}{4} = \frac{6l_2}{4\pi} \Rightarrow \frac{\pi l_1}{l_2} = 6$ 68. (a) $\frac{x(x+2)}{2} + \frac{\log |x-1|}{2} - \frac{\log |x^2+1|}{4} - \frac{\tan^{-1} x}{2} + c$ Explanation: $\int \frac{x^4}{(x-1)(x^2+1)} dx$ $=\int \frac{x^4-1}{(x-1)(x^2+1)}dx + \int \frac{1}{(x-1)(x^2+1)}dx$ $= \int \frac{(x+1)(x-1)(x^2+1)}{(x-1)(x^2+1)} dx + \int \frac{dx}{(x-1)(x^2+1)} dx$ $=\int (x+1)dx + \int \left[\frac{1}{2(x-1)} - \frac{x+1}{2(x^2+1)}\right] dx$ $= \int x dx + \int dx + \frac{1}{2} \int \frac{1}{x-1} dx - \frac{1}{4} \int \frac{2x}{x^2+1} dx - \frac{1}{2} \int \frac{1}{x^2+1} dx$ $=\frac{x^2}{2}+x+\frac{1}{2}\log|x-1|\frac{1}{4}\log|x^2+1|-\frac{1}{2}\tan^{-1}x+c$ 69. (c) 100 Explanation: 100 70. (d) a circle

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Explanation:

... The locus of middle point P(h, k) is $x^2 + y^2 = \frac{l^2}{4}$ which is the equation of a circle. 71.

(b)
$$x - 2y + 8 = 0$$

Explanation:
 $\begin{pmatrix} 1 \\ 2 \\ -2 \end{pmatrix}$

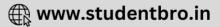
Let parabola $y^2 = 8x$ at point $(\frac{1}{2}, -2)$ is $(2t^2, 4t)$ $\Rightarrow t = \frac{-1}{2}$ Parameter of other end of focal chord is 2 So, coordinates of B is (8, 8) \Rightarrow Equation of tangent at B is 8y - 4(x + 8) = 0 $\Rightarrow 2y - x = 8$

$$\Rightarrow 2y - x = 0$$
$$\Rightarrow x - 2y + 8 = 0$$

72.

(d)
$$e^{x^2} (y^2 - 1) + e^{y^2} = C$$

Explanation: Let $y^2 = v \Rightarrow 2y \frac{dy}{dx} = \frac{dv}{dx}$
 $\Rightarrow (e^{x^2} + e^{v^2}) \frac{1}{2} (\frac{dy}{dx}) + e^{x^2} (xv - x) = 0$
 $\Rightarrow e^{x^2} + e^{V} + 2xe^{x^2} (v - 1) \frac{dx}{dv} = 0$...(i)
Let $e^{x^2} = t \Rightarrow 2xe^{x^2} \frac{dx}{dv} = \frac{dt}{dv}$
(i) $\Rightarrow t + e^{V} + (v - 1) \frac{dt}{dv} = 0$
 $\Rightarrow \frac{dt}{dv} + \frac{t}{v-1} = \frac{-e^v}{v-1}$ (Linear)
I.F. $= e^{\int \frac{1}{v-1} dv} = e^{\log(v-1)} = v - 1$



General solution of the given equation is

$$t(v - 1) = -\int e^{v} dv + c$$

$$\Rightarrow t (v - 1) = -e^{v} + c$$

$$\Rightarrow e^{x^{2}} (y^{2} - 1) = -e^{y^{2}} + c$$

$$\Rightarrow e^{x^{2}} (y^{2} - 1) = -e^{y^{2}} + c$$

73. (a) $\cos^{-1}(\frac{31}{49})$

Explanation: Direction ratios of the line joining (1, -2, 4) to (-1, 1, -2) are proportional to -2, 3, - 6

$$\cos \theta = \frac{|(2)(-2) + (3)(3) + (6)(-6)|}{\sqrt{2^2 + 3^2 + 6^2} \sqrt{(-2)^2 + 3^2 + (-6)^2}}$$
$$= \frac{31}{40}$$
$$\Rightarrow \theta = \cos^{-1}\left(\frac{31}{49}\right)$$

74.

(b) 3 **Explanation:** Let P is $\vec{0}$, Q is \vec{q} and R is \vec{r} , A is $\frac{2\vec{q}+\vec{r}}{3}$, B is $\frac{2\vec{r}}{3}$ and C is $\frac{\vec{q}}{3}$ Since, area of $\triangle PQR = \frac{1}{2} |\vec{q} \times \vec{r}|$ Area of $riangle \mathsf{ABC} = rac{1}{2} |\overrightarrow{AB} imes \overrightarrow{AC}|$ As $\overrightarrow{AB} = \frac{\overrightarrow{r} - 2 \overrightarrow{q}}{3}, \overrightarrow{AC} = \frac{-\overrightarrow{r} - \overrightarrow{q}}{3}$ So, Area of $\triangle \mathsf{ABC} = \frac{1}{6} |\overrightarrow{q} \times \overrightarrow{r}|$ Now, $\frac{\operatorname{Area}(\triangle PQR)}{\operatorname{Area}(\triangle ABC)} = 3$ 75. (c) $a\bar{x} + b$ **Explanation:** Required mean = $\frac{(ax_1+b)+(ax_2+b)+\ldots+(ax_n+b)}{n}$ $= \frac{a(x_1+x_2+\ldots+x_n)+nb}{n} = \mathsf{a}\bar{x} + \mathsf{b},$ $\left(\because rac{x_1+x_2+\ldots+x_n}{n} = ar{x}
ight)$

76.

(d) $\frac{99}{200}$

Explanation: If A draws 1, then B has options 2 to 100. If A draws 2, then B has options 3 to 100 and so on.

Required probability = $\frac{1}{100} \times \frac{99}{100} + \frac{1}{100} \times \frac{98}{100} + \ldots + \frac{1}{100} \cdot \frac{1}{100}$ $=\frac{1}{100} \times \frac{99+98+\ldots+1}{100} = \frac{99}{200}$

(d)
$$\frac{1}{2^{n/2}}$$

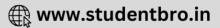
Explanation: —

Explanation:
$$\frac{1}{2^{n/2}}$$

78.

(b) y = x + 1**Explanation:** We have $\frac{x^2}{3} - \frac{y^2}{2} = 1$

Since, tangent is equally inclined to the axes i.e., $tan\theta = 1 = m$. Equation of tangent in slope form is



$$y = mx + \sqrt{a^2m^2 - b^2}$$

Here, $a^2 = 3$, $b^2 = 2$
 $\Rightarrow y = 1..x + \sqrt{3 \times (1)^2 - 2}$
 $\Rightarrow y = x + 1$
79.
(d) $B \cap C'$
Explanation: $(A \cup B \cup C) \cap (A \cap B' \cap C')' \cap C'$
 $= (A \cup B \cup C) \cap (A' \cup B \cup C) \cap C'$
 $= (A \cap A') \cup (B \cup C)] \cap C'$
 $= (A \cap A') \cup (B \cup C)] \cap C'$
 $= (A \cap A') \cup (B \cup C)] \cap C'$
 $= (B \cap C') \cup (C \cap C')$
 $= (B \cap C') \cup \phi$
 $= B \cap C'$
80. (a) $-2 - \sqrt{3}$
Explanation: Since the given determinant is equal to zero
 $\Rightarrow 0 (0 - \cos x \sin x) - \cos x (0 - \cos^2 x) - \sin x(\sin^2 x - 0) = 0$
 $\Rightarrow \cos^3 x - \sin^3 x = 0$
 $\Rightarrow \tan^3 = 1 \Rightarrow \tan x = 1$
 $\therefore \sum_{x \in s} \tan(\frac{\pi}{3} + x) = \sum_{x \in S} \frac{\tan \pi/3 + \tan x}{1 - \tan \pi/3 \cdot \tan x}$

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Explanation:

 $= -2 - \sqrt{3}$

81.9

 $\sum_{x \in s} \frac{\sqrt{3}+1}{1-\sqrt{3}}$

Given
$$f^{3}(x) = = \int_{0}^{x} t f^{2}(t) dt ...(i)$$

 $\sum_{x \in s} \frac{\sqrt{3}+1}{1-\sqrt{3}} \times \frac{1+\sqrt{3}}{1+\sqrt{3}} \Rightarrow \sum_{x \in s} \frac{1+3+2\sqrt{3}}{-2}$

Differentiating both the sides of equation (i) by using Leibnitz rule, we get $3f^2(x) f'(x) = x f^2(x)$ As f(x) is strictly increasing, so f(x) $\neq 0$ $\therefore 3 f'(x) = x \Rightarrow f'(x) = \frac{x}{3}$ $\therefore f(x) = \frac{x^2}{6} + C$ (On integrating both sides with respect to x.) But f(0) = 0 $\Rightarrow C = 0$ $\therefore f(x) = \frac{x^2}{6}, x \ge 0$ Slope of the tangent at P(x₁, y₁) to the curve f(x) = $\frac{x_1}{3}$ \therefore Slope of normal = $\frac{-3}{x_1}$ i.e., $\frac{-1}{2} = \frac{-3}{x_1}$ (Given) $\Rightarrow x_1 = 6$ and $y_1 = 6$ So, Equation of normal is (y - 6) = $\frac{-1}{2}$ (x - 6) \therefore For y-intercept, put x = 0, we get y = 9 82. 16 Explanation:

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 $a^{3}(x) - (x^{3} + 2)a^{2}(x) + (2x^{3} + 1)a(x) - x^{3} = 0$ \Rightarrow (q(x) - 1)² q(x) - x³) = 0 So, invertible function is $q(x) = x^3$ $a^{-1}(x) = x^{1/3}$ $g'(8) \cdot (g^{-1})'(8) = 16$ 83.285.0 **Explanation:** $[ec{\mathbf{b}}\cdot(ec{\mathbf{a}} imesec{\mathbf{c}})]^2=[ec{\mathbf{a}}\cdot(ec{\mathbf{b}} imesec{\mathbf{c}})]^2$ $=egin{array}{cccc} a^2 & ec{a}.ec{b} & ec{a}\cdotec{c} \ ec{b}.ec{a} & b^2 & ec{b}.ec{c} \ ec{c} & ec{a} & ec{c}\cdotec{b} & c^2 \end{array}$ As $ert ec a ert = 14, ec b ert = \sqrt{3}, ec a \cdot ec b = 0$ $ec{a}.ec{c}=11,ec{b}.ec{c}=-\sqrt{3}|b|=-\sqrt{3} imes\sqrt{3}=-3$ & $ec{b}.\,(ar{a} imesec{c})=27$ $\Rightarrow (27)^2 = egin{bmatrix} 14 & 0 & 11 \ 0 & 3 & -3 \ 11 & -3 & c^2 \end{bmatrix}$ $\Rightarrow 14 \left(3c^2 - 9
ight) + 11(-33) = 729 \Rightarrow c^2 = 29$ So, $|ec{a} imesec{c}|^2 = a^2c^2 - (ec{a}\cdotec{c})^2 = 14 imes29 - 11^2 = 285$ 84.27.0 **Explanation:** $|x^2-2| \leq y \leq x$ $A = \int\limits_{1}^{\sqrt{2}} \left(x - \left(2 - x^2
ight)
ight) dx + \int\limits_{\sqrt{2}}^{2} \left(x - \left(x^2 - 2
ight)
ight) dx$ $x = \left[rac{x^2}{2} - 2x + rac{x^3}{3}
ight]_1^{\sqrt{2}} + \left[rac{x^2}{2} - rac{x^3}{3} + 2x
ight]_{\sqrt{2}}^2$ $=\left(1-2\sqrt{2}+rac{2\sqrt{2}}{3}
ight)-(rac{1}{2}-2+rac{1}{3})+(2-rac{8}{3}+4)-\left(1-rac{2\sqrt{2}}{3}+2\sqrt{2}
ight)$ $=-4\sqrt{2}+\frac{4\sqrt{2}}{3}+\frac{7}{6}+\frac{10}{3}=\frac{-8\sqrt{2}}{3}+\frac{9}{2}$ Then $6A = -16\sqrt{2} + 27 \therefore 6A + 16\sqrt{2} = 27$ 85.14.0 **Explanation:** Shortest distance between the lines Since $\vec{a}_1 = (2, -1, 6), \vec{a}_2 = (6, 1, -8)$ and

 $\vec{b}_1 = (3, 2, 2), \vec{b}_2 = (3, -2, 0)$ Now $(\vec{a}_2 - \vec{a}_1) = (4, 2, -14)$ $\vec{b}_1 \times \vec{b}_2$ = (4, 6, -12) So, shortest distance = $\left| \frac{(\vec{a}_2 - \vec{a}_1)(\vec{b}_1 \times \vec{b}_2)}{|\vec{b}_1 \times \vec{b}_2|} \right|$ $= \left| \frac{16+12+168}{\sqrt{16+36+144}} \right| = \left| \frac{196}{14} \right| = 14$ 86.17 **Explanation:** n(S) = 36Let E be the event of getting the sum of digits on the dice equal to 7, then n(E) = 6 $P(E) = \frac{6}{36} = \frac{1}{6} = P$ then P(E') = q = $\frac{5}{6}$ probability of not throwing the sum 7 in first m trails = q^{m} Therefore P(at least one 7 in m throw) = 1 - q^{m} = 1 - $\left(\frac{5}{6}\right)^{m}$ According to the question $1 - \left(\frac{5}{6}\right)^{m} > 0.95 \Rightarrow \left(\frac{5}{6}\right)^{m} > 0.05$ \Rightarrow m(log₁₀5 - log₁₀6) < log₁₀1 - log₁₀20 ∴ m > 16.44 Hence, the least number of trails = 1787.5 **Explanation:** 5 88.16 **Explanation:** $\tan A \cdot \tan B = \frac{1}{2}$ $\Rightarrow an A = rac{1}{2 an B}$ $\Rightarrow an^2 A = rac{1}{4 an^2 B}$ Now, $(5 - 3 \cos 2A)(5 - 3 \cos 2B)$ $= \left(5 - 3\left(\frac{1 - \tan^2 A}{1 + \tan^2 A}\right)\right) \left(5 - 3\left(\frac{1 - \tan^2 B}{1 + \tan^2 B}\right)\right)$ $= \left(\frac{5 + 5\tan^2 A - 3 + 3\tan^2 A}{1 + \tan^2 A}\right) \left(\frac{5 + 5\tan^2 B - 3 + 3\tan^2 B}{1 + \tan^2 B}\right)$ $= \left(\frac{2+8\tan^2 A}{1+\tan^2 A}\right) \left(\frac{2+8\tan^2 B}{1+\tan^2 B}\right)$ $= 4 \times \left(\frac{1+4\tan^2 A}{1+\tan^2 A}\right) \left(\frac{1+4\tan^2 B}{1+\tan^2 B}\right)$ $= 4 \times \left(\frac{1+4\left(\frac{1}{4\tan^2 B}\right)}{1+\left(\frac{1}{2}\right)}\right) \left(\frac{1+4\tan^2 B}{1+\tan^2 B}\right)$ $= 4 \times \left(\frac{4(1+\tan^2 B)}{1+4\tan^2 B}\right) \left(\frac{1+4\tan^2 B}{1+\tan^2 B}\right)$ = 4 × 4 = 16 89.8.0 **Explanation:**

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Given that $(I - A)^2 = I^3 - A^3 - 3A(I - A) = I - A^3$ \Rightarrow 3A(I - A) = 0 \Rightarrow A² = A $\Rightarrow \begin{bmatrix} a^2 & ab + bd \\ 0 & d^2 \end{bmatrix} = \begin{bmatrix} a & b \\ 0 & d \end{bmatrix}$ \Rightarrow a² = a, b(a + d - 1) = 0, d² = d **Case I:** $b = 0 \Rightarrow (a, d) = (0, 1), (0, 0), (1, 1), (1, 0) \rightarrow 4$ ways **Case II:** a + d = 1 \Rightarrow (1, 0), (0, 1) and b = $\pm 1 \rightarrow 4$ ways \Rightarrow Total 8 matrices 90.3 **Explanation:** For x-intercept y = 0||x-2|-a| = 3 $\Rightarrow |x-2|$ - a = 3 or -3 $\Rightarrow |x-2| = a + 3 \text{ or } a - 3$ For 3x-intercepts a + 3 > 0 and a - 3 = 0 ...(i) or a + 3 = 0 and a - 3 > 0 ...(ii) From Eq. (i) a = 3 and Eq. (ii) is rejected. Hence, sum = 3



